Challenges in Teaching Real Analysis classes at University of PGRI, South Sumatra, Indonesia

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Abstract

This paper discusses our experience and challenges in teaching advanced undergraduate Real Analysis classes for Mathematics Education students at University of PGRI (\textit{Persatuan Guru Republik Indonesia}) Palembang, South Sumatra, Indonesia. We observe that the syllabus contains topics with a high level of difficulty for the students who are specialized in education and intend to teach mathematics at the secondary level. The conventional lecturing method is mainly implemented during the class, with some possible variations of the method, including the Texas method (also known as Moore’s method) and the small group guided discovery method. In particular, the latter method has been implemented successfully for a Real Analysis class at Darmouth College, New Hampshire by Dumitras\c{c}u in 2006. Although it is a real challenge to apply a specific teaching method that will be able to accommodate a large number of students, the existing teaching activities can still be improved and a more effective method could be implemented in the future. Furthermore, the curriculum contents should be adapted for an audience in mathematics education to equip them for their future career as mathematics teachers. Any constructive suggestions are welcome for the improvement of our mathematics education system at the university as well as in the national scale.

1 Introduction

There are a number of teaching methods and certainly teaching style varies from one lecturer to another. Several ways of teaching method which are commonly carried out in many parts of the world include the following: questioning, explaining, demonstrating, collaborating and learning by teaching [1]. In particular, the learning by teaching (German, \textit{Lernen durch Lehren}) is a widespread method in Germany, where the students take the teacher’s role and teach their peers.

More specific, we want to use certain methods in teaching mathematics, and in this context, in teaching Real Analysis classes. Methods of teaching mathematics include the following: classical education, rote learning, exercises, problem solving,
new math, historical method and reform or standard-based mathematics [2]. In particular, there are a significant research results on the implementation of the realistic mathematics education method in Indonesia [3, 4, 5, 6]. Furthermore, cooperative learning methods are now being used more and more often in teaching undergraduate mathematics and science [7, 8, 9, 10] as well as in higher education setting [11].

Another teaching method which accompanies a conventional instruction method is known as the guided discovery method. In this method, the students learn through personal experience . . . with limited guidance from the lecturer, . . . thought provoking topics are introduced as questions for investigation by the students [12, 13]. An experience of implementing teaching method using a combination of guided discovery, lecturing and group work in an undergraduate Real Analysis class has been proven to improve students’ understanding [14]. The author concludes that the guided discovery method is an excellent modality of exposing students to mathematical research.

We observe that a conventional teaching method using instruction and lecturing for the Real Analysis course presents a challenge for the students who are specialized in Mathematics Education. This challenge motivates us in bringing this problem into the surface.

What is real analysis and what are the scope of the course on Real Analysis? Real analysis is a branch of mathematical analysis dealing with the set of real numbers. In particular, it deals with the analytic properties of real functions and sequences, including convergence and limits of sequences of real numbers, the calculus of the real numbers and continuity, smoothness and related properties of real-valued functions [15]. Certainly a course on Real Analysis should cover the aforementioned materials. This course is an important component of mathematics curriculum for both educational and noneducational streams at the undergraduate level.

This paper is organized as follows. Section 2 discusses the organization of the courses, including reference textbooks being used and the method of assessment. Section 3 explains challenges and difficulties that students face in following the classes. Furthermore, Section 4 discusses our observations in conducting the classes and implementing several teaching methods. This section also provides the students’ responses toward different teaching methods. Finally, Section 5 gives the conclusion and remark for future research to our discussion.

2 Organization of the courses

The classes of Real Analysis I and II are compulsory subjects for undergraduate students in Mathematics Education at University of PGRI (Persatuan Guru Republik Indonesia), Palembang, South Sumatra, Indonesia. These courses carry three credit points and are given to the third year students or on the fifth and the sixth semesters of their study. There is only one time interaction every week and it lasts for 150 minutes, that is three times 50 minutes.

The materials covered in Real Analysis II are Euclidean space, metric space, topological concept in metric space, set theory and metric spaces, Riemann integral and Riemann-Stieltjes integral. The first three topics are materials covered in Real Analysis I. We find it redundant that one course is the subset of the other, with
fifty percent of intersection from Real Analysis II.

The number of students in one class ranges from 15 up to 40 students and there are 9 parallel classes for the same course with total number of 335 students. One senior lecturer plays a role as a coordinator for three other lecturers. Practically, the material presented in this paper is merely based our observation on three different classes taught by one of us (ES). One class consists with only 15 students while the other two are 27 and 30 students, respectively.

Lecture notes are prepared and compiled from several mathematical analysis books, among others are Introduction to Real Analysis by R. G. Bartle and D. R. Sherbert [16], Principles of Mathematical Analysis by W. Rudin [17], Pengantar Analisis Real by S. Darmawijaya [18] and lecture notes on Real Analysis from Malang State University, East Java, Indonesia. For Real Analysis II, additional references have been used, among others are Analisis Real by R. Soemantri [19], Real Analysis by H. L. Royden [20] and Fundamental Concepts of Analysis by A. H. Smith and W. A. Albrecht, Jr., [21].

The method of assessment is based on several components with different weighting. One coursework is assigned and is graded on an individual basis, this assignment carries 20 percent of the final grade. Two examinations, the mid-semester and the final exams, carry 30 and 50 percent of the final grade, respectively.

3 Students’ difficulties

It is mentioned in the previous section that there is an overlapping of the material within the courses Real Analysis I and II. Although the students have learned some of the materials earlier, when we come to the sixth semester, it seems that many have forgotten as if they never taken a course on Real Analysis.

Many students have a wrong interpretation on what mathematics subjects involve. They generally associate mathematics with counting, calculation and computation which in turn restrict the discipline into only arithmetic. In fact, one online encyclopedia defines mathematics as the body of knowledge centered on such concepts as quantity, structure, space and change and also the academic discipline that studies them [22]. That is why mathematics includes the use of abstraction and logical reasoning which involves rigorous deduction from appropriately chosen axioms and definitions.

We observe that the students are less familiar with theorems and how to prove them. Implementing mathematics symbols and terminologies is far from familiar. The concept of set theory is still weakly comprehended. As an example, many students are not able to distinguish simple notations such as $(a, b)$, $[a, b)$, $(a, b]$ and $\{a, b\}$. In particular, the students consider proving theorems, convergence and Riemann integral as the most difficult topics. Bear in mind that the students who specialize in Mathematics Education spend only merely of 55% from the total credit points on Mathematics courses for the entire study period, i.e. 84 out of 154 credit points are Mathematics courses.

Furthermore, the students also face difficulties in some technical issues, in particular to find the literature. It is rather difficult to obtain the reference books since the library has a limited amount of these books while the number of students are quite massive. The price of these textbooks are considered very expensive for all
of the students. Even if the students possess textbooks, yet, since English is not
the mother tongue of students, language barrier may present another significant
challenge in understanding the material.

4 Observations and students’ responses

We have implemented several teaching methods in conducting the Real Analysis
classes. These are the conventional instruction method, Moore’s method and the
guided discovery method. The conventional instruction method is implemented
to the majority of the class sessions, in particular to explain definitions and new
corcepts. Moore’s method is implemented when explaining the properties of integral.
For instance, this method is used to prove the following theorem. If $f$ is a bounded
function and Darboux integrable on an interval $[a, b]$, show that $f^2$ is also Darboux
integrable on the same interval. The guided discovery method is also implemented
in a number of theorem proving.

We observe that the students prefer more the conventional instruction method
than the other two methods. The students are not able to follow Moore’s method
at all since none of them is able to answer or to give an idea in solving the theorem
above. It is observed that a small number of the students are able to follow the
guided discovery method, i.e. less than 20%. Regarding the preference of teaching
method, 34.6% of the students prefers the conventional instruction method where
the teacher only lecturing, 32.7% prefers a variation in teaching method, 13.5%
prefers the conventional instruction and discussion, 5.8% prefers the guided discovery
method, 5.8% prefers the conventional instruction and problem solving and 1.9%
each for preference in question and answer session, task assignment, discussion and
self-study.

Regarding the implementation of different teaching methods in understanding
the material, 48% of the students considers it helpful, 21.2% also considers it helpful
but prefer only the conventional instruction method, 5.8% says it can be helpful
but without discussion session, 9.6% considers it is not helpful at all and 15.4%
says it depends on the material being covered. Furthermore, we would like to know
what kind of comprehension the students acquire after completing the courses on
Real Analysis. Almost 40% of the students (39.4%) acquires logical reasoning and
improvement in theorem proving, 30.3% acquires knowledge on the topic of integral,
18.2% improves their understanding in mathematical symbols and 12.12% claims
does not improve at all.

Regarding the material delivery by the lecturer, almost 60% says that it is very
easy to understand (59.6%), 32.7% responses that it is sufficiently easy to understand
and only 7.7% says that it is difficult to understand. Regarding the availability of
the textbooks, an excellent number of 94.2% claims that it is very helpful, 3.8% says
that it is helpful but they need some other additional references and 9.6% says that
it is not really helpful. The following section gives conclusion to our discussion.
5 Conclusions

We have discussed that Real Analysis courses are very important components in the curriculum of Mathematics Education programme. Nevertheless, a majority of the students consider that these courses are very tough and challenging. We have implemented different teaching methods to help the students to get better understanding of the material. Even though Moore’s method and the guided discovery method have been implemented successfully in a number of mathematics courses in the US, we observe that these methods are still difficult to be implemented for the Real Analysis courses in particular at the University of PGRI, Palembang, Indonesia. Apart from implementing excellent teaching methods, we strongly believe that the curriculum for these courses should be adapted to the characteristics of students who are specialized in Mathematics Education and their career after completing their degree. For future research, it is important to investigate the significant value of the students’ response. This also involves the quantitative calculation and validation test. Another research direction is to implement teaching method that relates the topics with the materials in secondary school since the students will eventually become secondary school teachers themselves anyway.

References

http://clte.asu.edu/active/clinhighed.pdf


http://math.arizona.edu/~dumitras/k/preprints/guided-D.pdf


[18] S. Darmawijaya. *Pengantar Analisis Real*. Faculty of Mathematics and Natural Sciences, Gadjah Mada University, Yogyakarta, 19??.


